



# **Automated adjustment of voxel-dependent importance factors in inverse planning**

Sebastiaan Breedveld, Pascal Storch,  
Marleen Keijzer, Ben Heijmen

as presented on the XVth ICCR 2007 in Toronto, Canada

# Constrained inverse planning

Find a fluence resulting in a dose distribution satisfying (hard) dose-volume and maximum-dose constraints, e.g.:

- minimum-dose PTV  $> 50$  Gy
- maximum-dose dose Spinal Cord  $< 45$  Gy
- dose-volume Bowel at 35 Gy  $< 25\%$

# Beam profile objective function

$$\min_f \sum_{v \in \text{volumes}} \xi_v (Hf - d_v^p)^T \eta_v (Hf - d_v^p) + \kappa (Mf)^T (Mf)$$

volume wide  
importance  
factor

dose resulting  
from fluence  $f$

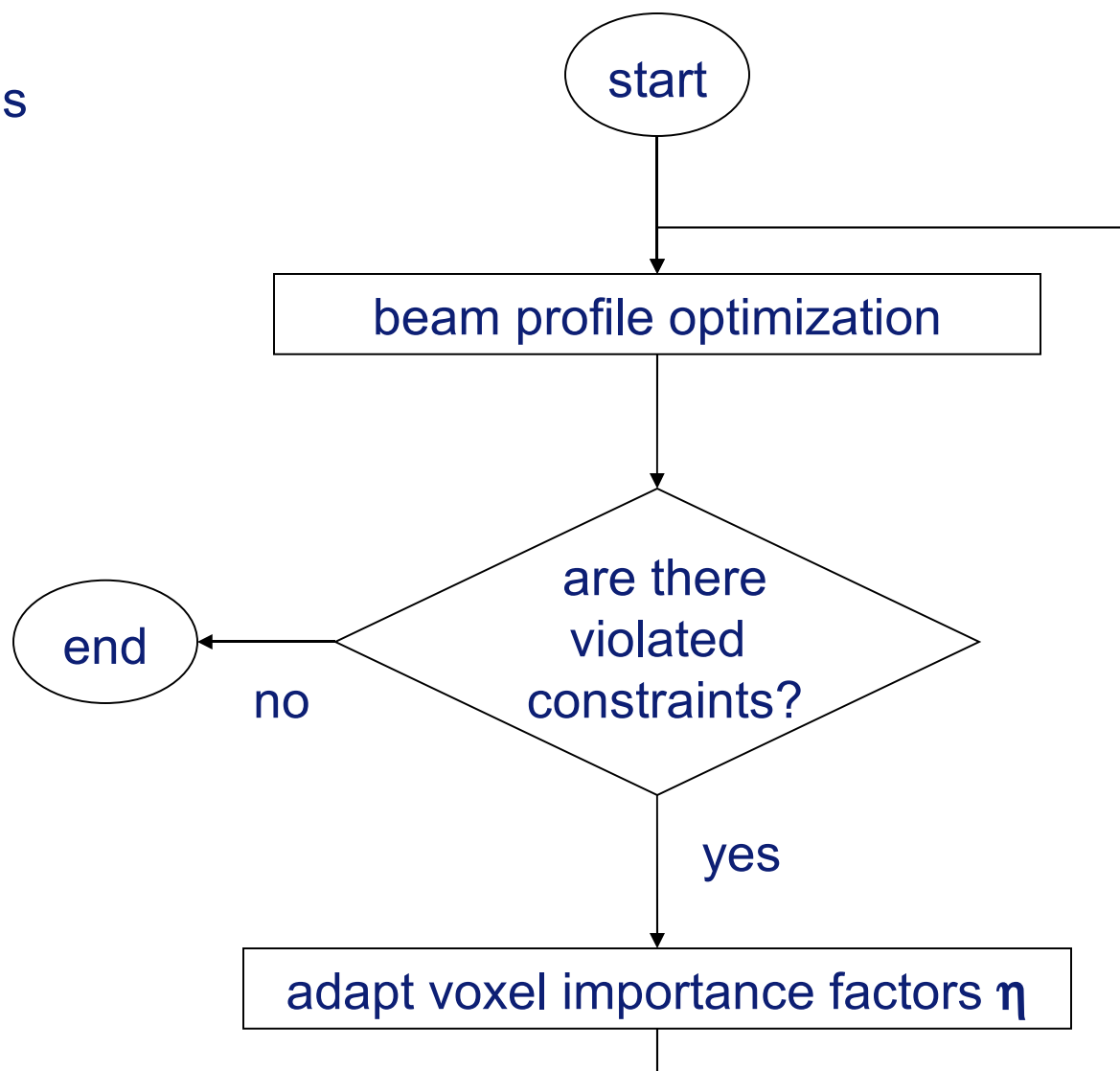
prescribed dose  
for volume

diagonal matrix with  
**voxel-dependent  
importance factors**  
for volume  $v$

term to enforce  
smooth fluences

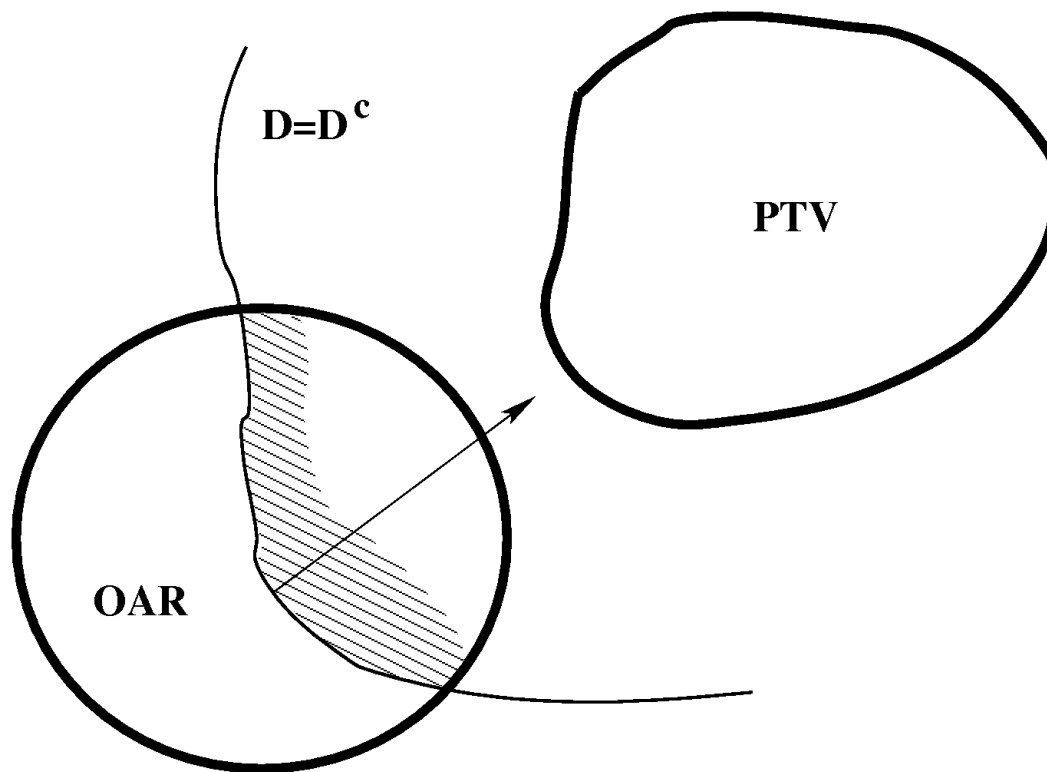
# Constrained inverse planning

2 step process



## Voxel adaption – how to select?

- increasing the weight of a voxel *encourages* the beam profile optimization to meet the prescribed dose
- select voxels which do not meet their constraints



# Moving on...

So far:

- algorithm optimizes on hard constraints

But:

- fails to come up with a solution when constraints are too tight
- does not necessarily give a better solution if possible

So:

- what are the most optimal constraints?

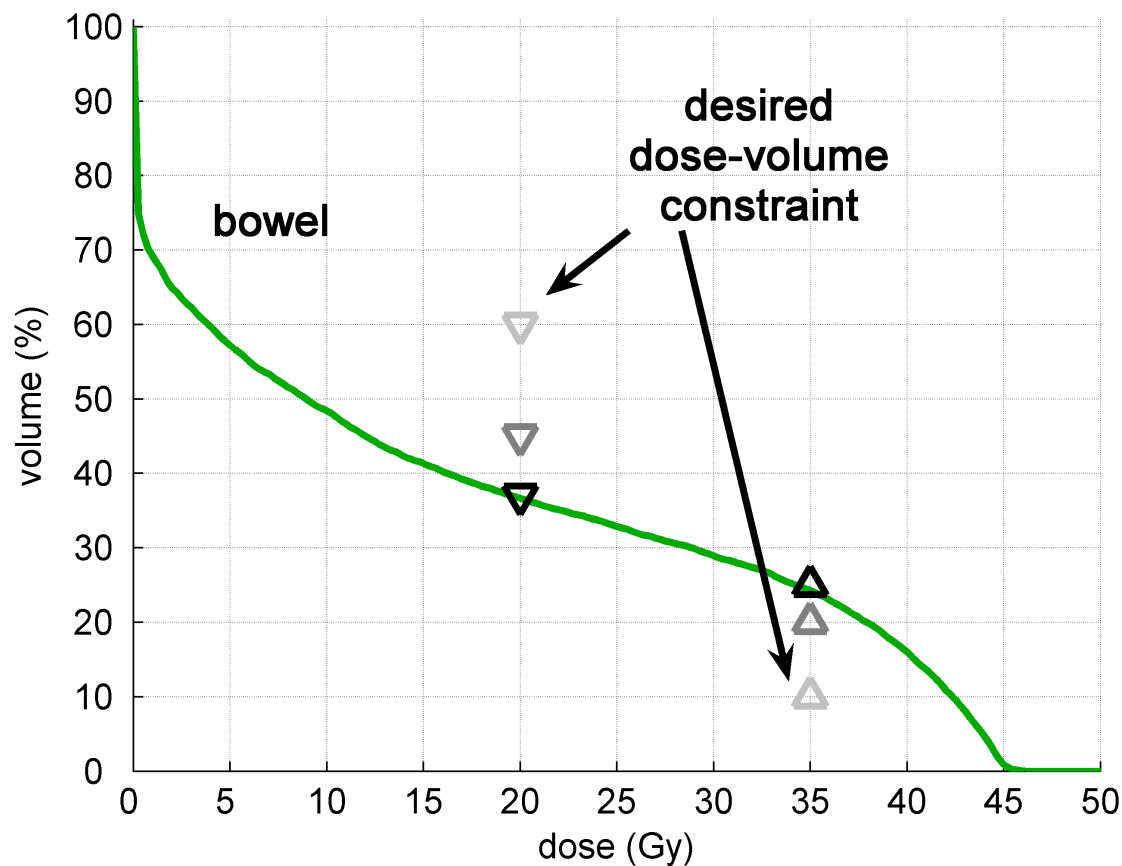
# Moving on... to Pareto optimality

Use a list of constraints ranked to priority:

- first meet all hard constraints
- try to meet more important constraints prior to less important constraints
- relax constraints if necessary, tighten is possible

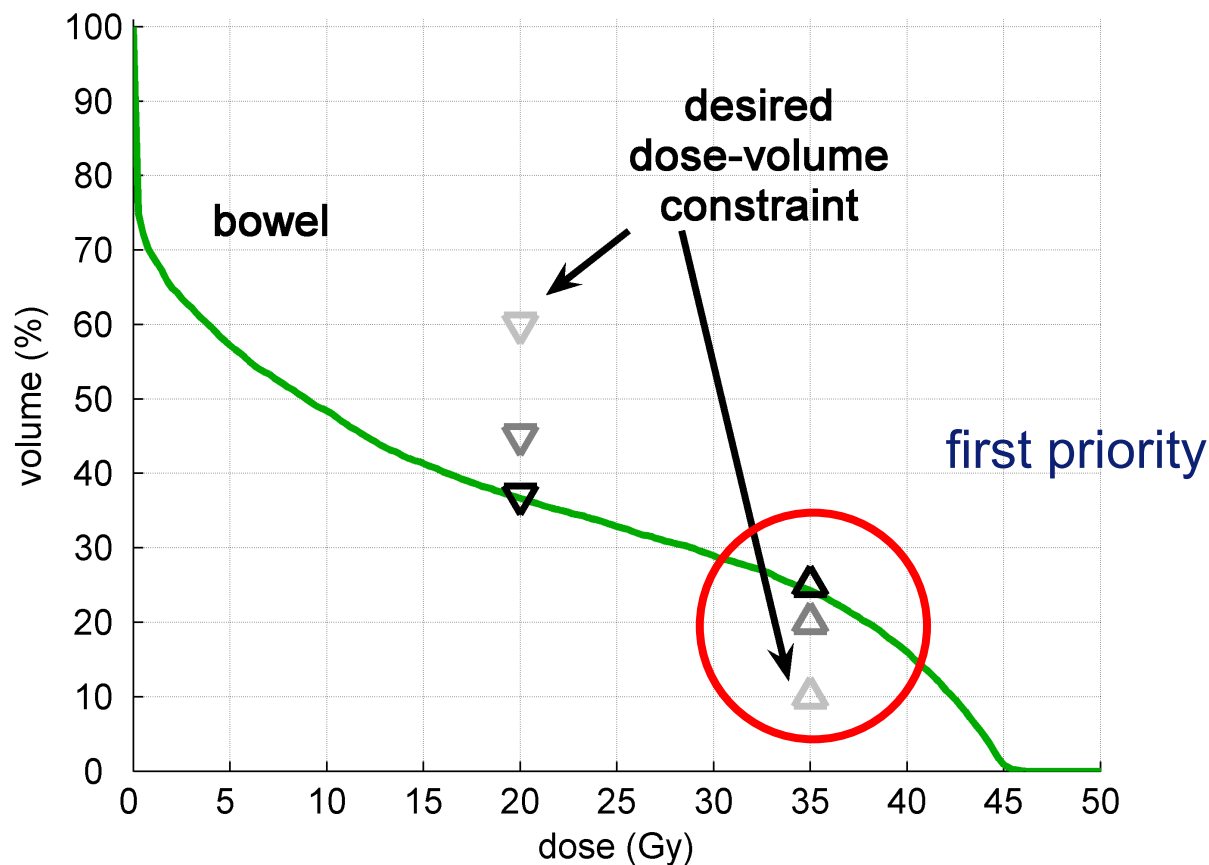
no	volume	constraint	critical dose	objective	constraint
		type			set
1	PTV	DV	42.42 Gy	100%	0
2	PTV	Max		47.78 Gy	0
3	Body	Max		47.78 Gy	0
4	Bowel	DV	35 Gy	20%	1
5	Bladder	DV	40 Gy	40%	2
6	Colon	DV	40 Gy	20%	2
7	Bowel	DV	20 Gy	50%	3
8	Bladder	DV	20 Gy	75%	3
9	Colon	DV	20 Gy	30%	3
10	Body	DV	30 Gy	40%	4

# Example relaxation and tightening

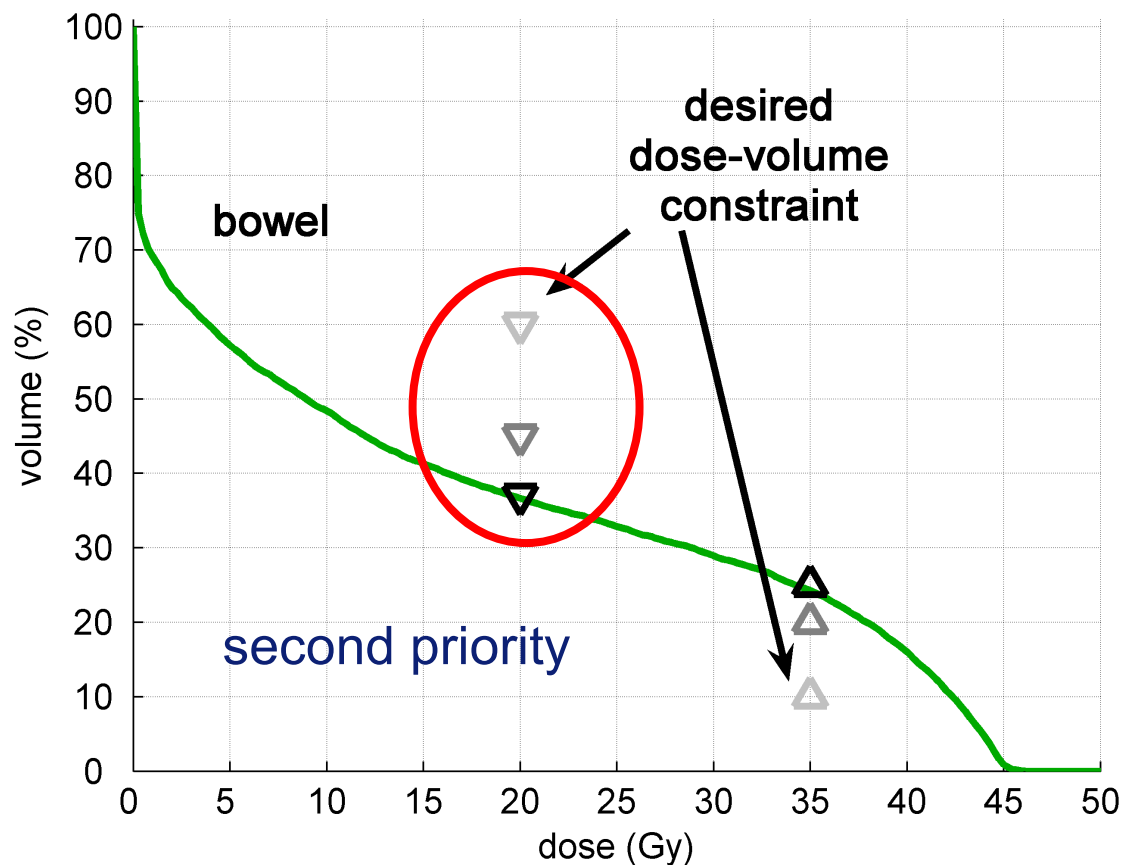




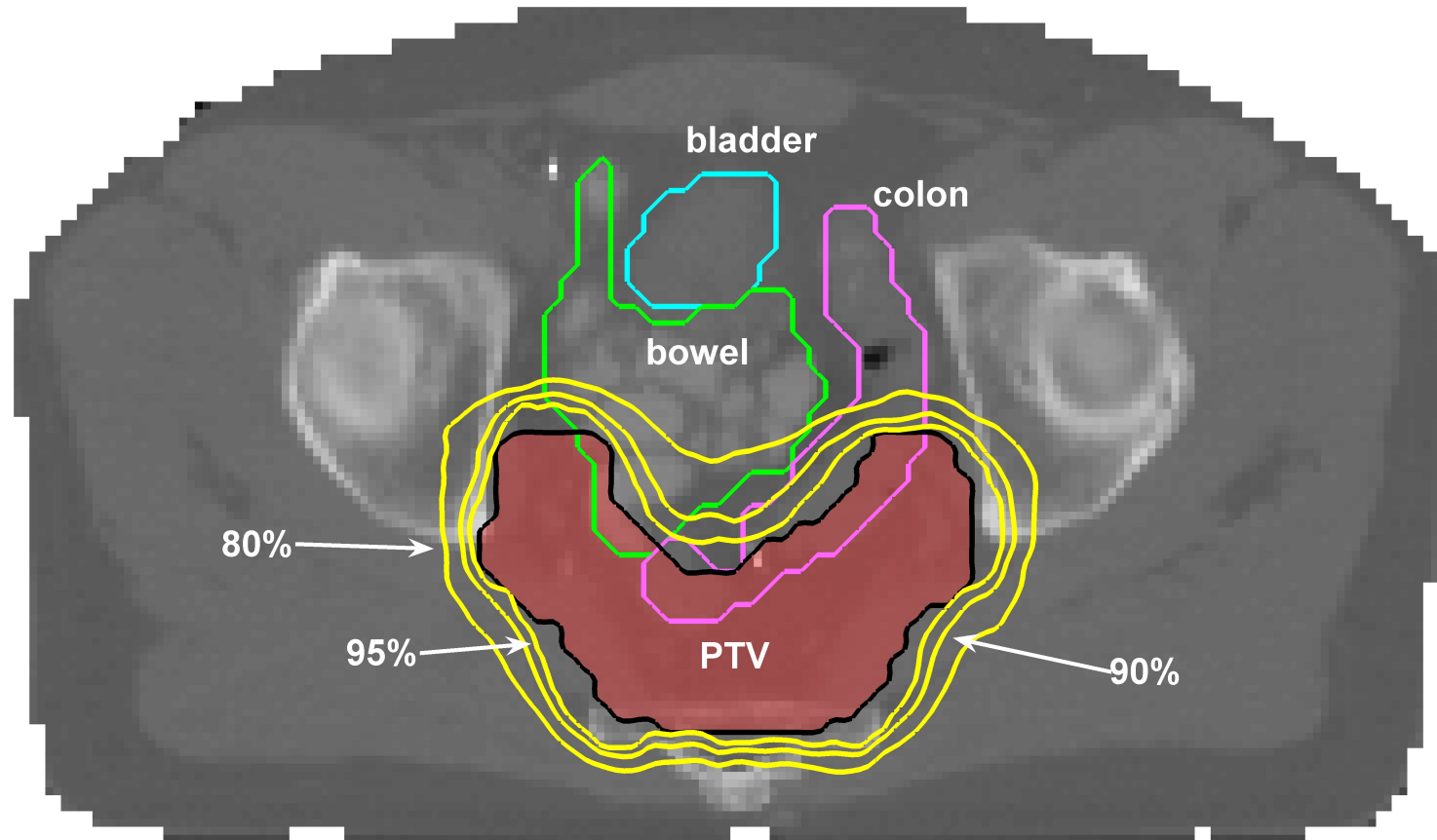
# Example relaxation and tightening



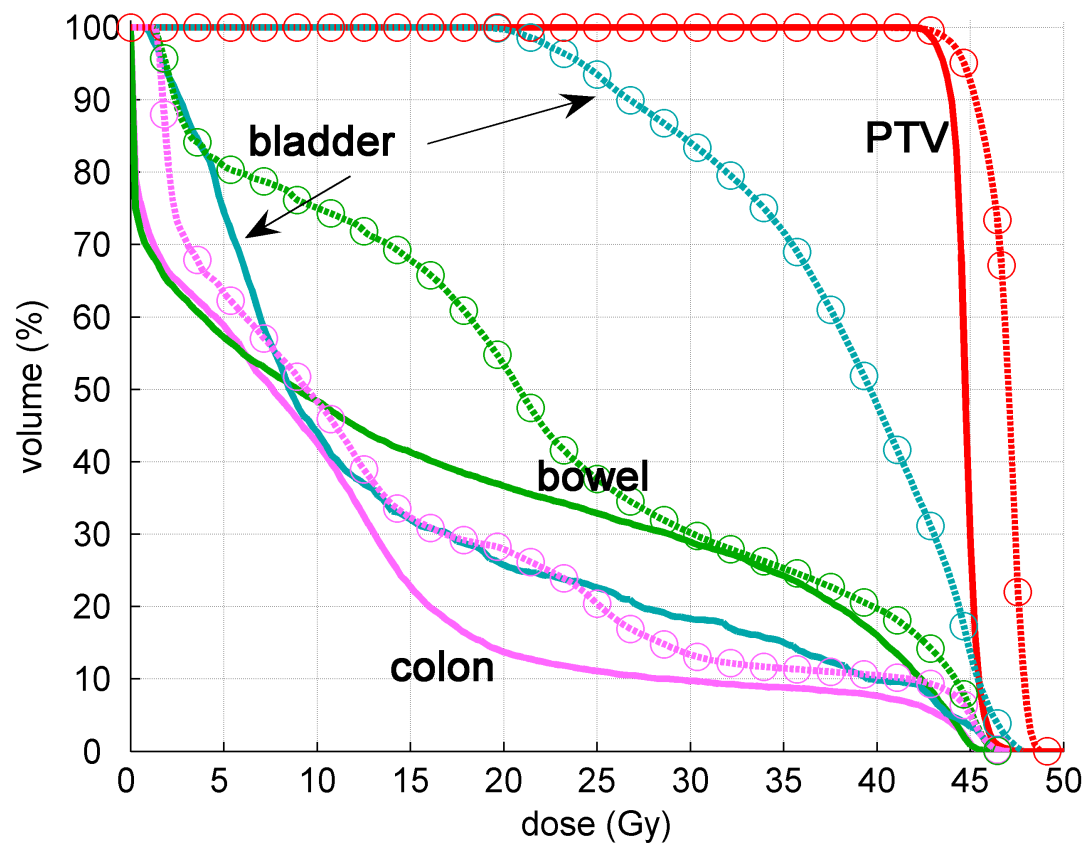
# Example relaxation and tightening



## Results: Rectum



# Results: Rectum

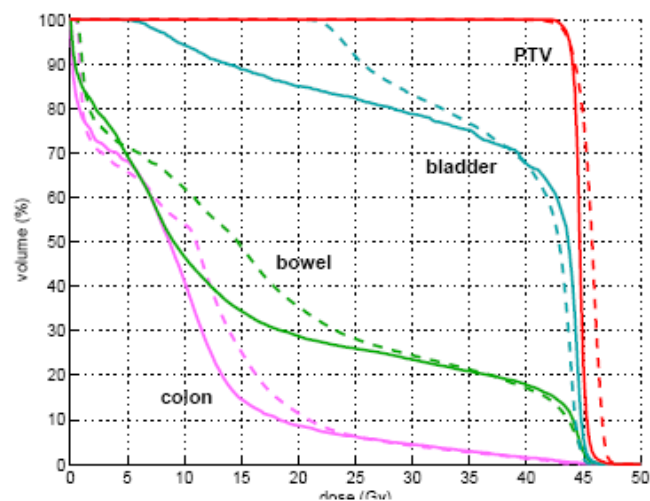
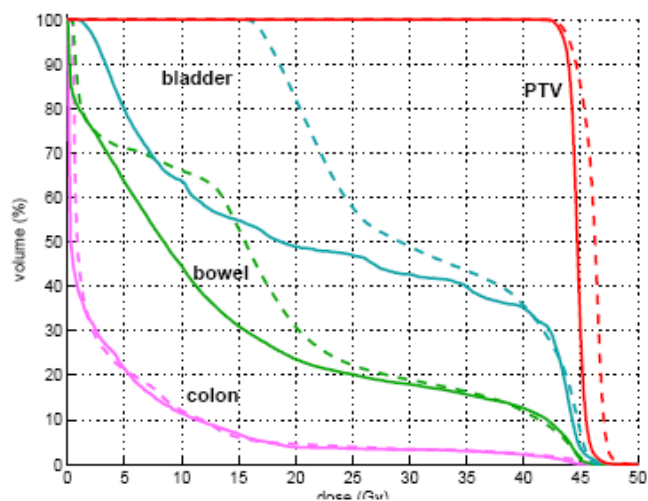
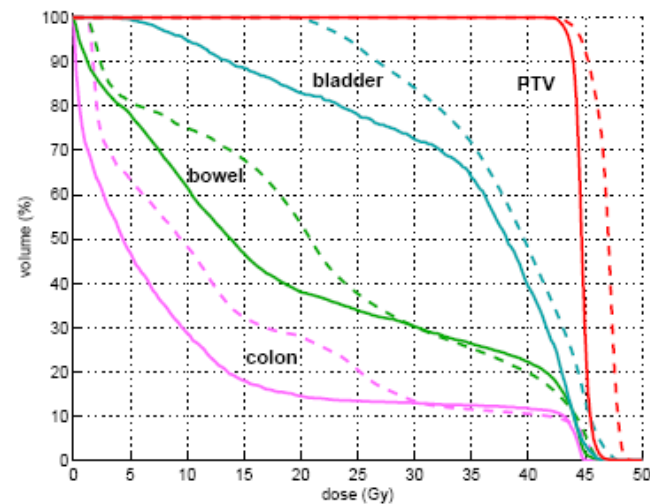
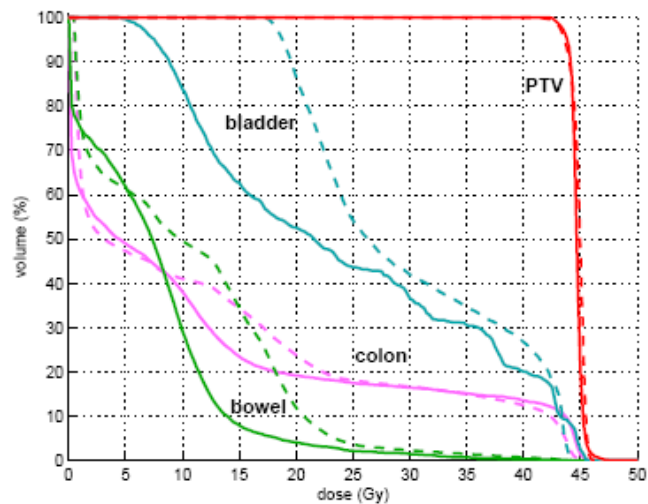


# Class solutions

A well defined list of constraints can be used as a class solution.

Research on 8 rectum patients and 5 oropharynx patients  
show structural and significant improvements.

# Class solutions



# Performance and characteristics

Direct optimization on constraints that are already Pareto optimal:

41 minutes

Optimization to find Pareto optimal constraints (from scratch):

58 minutes

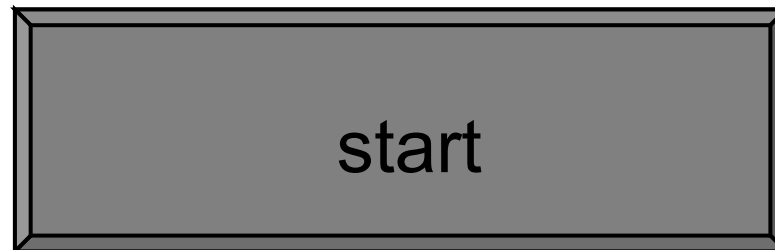
**Solutions are identical!**

(except for some numerical noise)

# Performance and characteristics

Optimization time can be further reduced by parallelization of the beam profile optimization algorithm. Using two threads on a SMP machine gives an speed-up of over 90%

Optimization is also 'labour-free' because no interaction is needed when an ordered constraint list is used.





# Summary and conclusions

We developed an algorithm to automatically adapt voxel-dependent importance factors for optimization on (hard) dose-volume and maximum-dose constraints.

By using a priority constraint list, constraints are optimized in priority to find a Pareto optimal set of constraints.

(Soft) constraints can be relaxed if necessary and tightened if possible.

The prioritized constraint list can be used as a class solution.

For rectum and oropharynx patients it shows consequently significantly better solutions than the manually optimized clinical plans.